

## Investigation of Modulation Techniques for Parametric Underwater Communications

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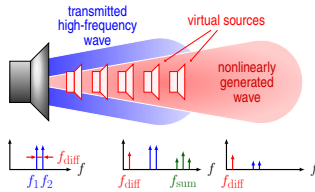
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# Investigation of Modulation Techniques for Parametric Underwater Communications

## Motivation

- **approach:** exploit nonlinearly generated wave components for communication purposes
- **principle:** bases on the parametric array [1]:



- transmission of a high-frequency acoustic wave
- intermodulation within the transmitted wave during the wave propagation in fluid media
- new frequency components are nonlinearly generated
- low frequency components are used for communication purposes

- **key properties of the nonlinearly generated low frequency wave for underwater communications:**

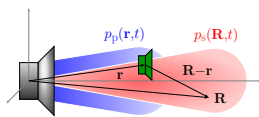
- + high directivity
- mitigation of Doppler and delay spread
- + low center frequency
- long-range communication
- + high relative bandwidth
- increase in data rate
- conversion loss
- long-range communication
- nonlinear signal distortions
- requires specific modulation techniques

## Physical Modelling

- fluid described by:
  - equilibrium state variables:  $p_0, \rho_0$  and  $\mathbf{v}_0$  (assumption: quiescent fluid  $\mathbf{v}_0 = 0$ )
  - disturbances:  $p, \rho$  and  $\mathbf{v}$
- dependencies of these state variables are formulated in the basic set of equations (assumption: ideal fluid):
  - $\frac{\partial \rho}{\partial t} = -\text{div}\{(\rho_0 + \rho)\mathbf{v}\}$  (1) equation of continuity
  - $\frac{\partial}{\partial t}\{(\rho_0 + \rho)\mathbf{v}\} + (\text{div}\{(\rho_0 + \rho)\mathbf{v}\cdot\mathbf{v}^T\})^T + \text{grad}\{p\} = 0$  (2) equation of motion
  - $\rho = \hat{\rho}(p, p_0, \rho_0)$  (3) equation of state (assumption: isentropic process)
- a second-order approximation of the basic set of equations followed by substitutions and manipulations gives:

$$\frac{1}{c_0^2} \frac{\partial^2 p(\mathbf{r}, t)}{\partial t^2} - \Delta p(\mathbf{r}, t) - \alpha \frac{\partial^2 p(\mathbf{r}, t)^2}{\partial t^2} = 0$$

- a quasi-linear approach is considered to simplify the nonlinear second-order-wave equation:



$$p(\mathbf{R}, t) \approx \varepsilon p_p(\mathbf{R}, t) + \varepsilon^2 p_s(\mathbf{R}, t)$$

$\varepsilon \ll 1$

- transmitted high frequency wave:
  - denoted as primary wave  $p_p$
  - propagates approximately linearly
  - creates virtual sources, which radiate the new frequency components
- nonlinearly generated frequency components:
  - denoted as secondary wave  $p_s$
  - assumed to propagate linearly
  - creates no further virtual sources
- motivates the use of the perturbation theory

- using the perturbation theory and equating the coefficients yield two linear wave equations:

- linear wave equation for the primary wave  $p_p$ :

$$\frac{1}{c_0^2} \frac{\partial^2 p_p}{\partial t^2} - \Delta p_p = 0$$

- linear, inhomogeneous wave equation for the secondary wave  $p_s$ :

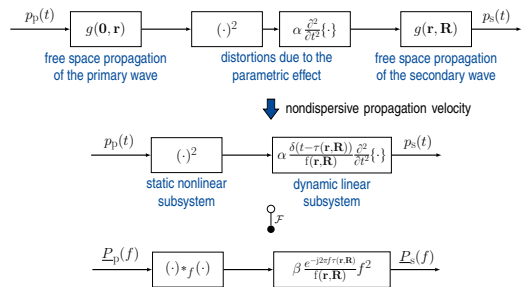
$$\frac{1}{c_0^2} \frac{\partial^2 p_s}{\partial t^2} - \Delta p_s = \alpha \frac{\partial^2 p_p^2}{\partial t^2}$$

- solution for the secondary wave with Green's function  $g(\cdot)$ :

$$p_s(\mathbf{R}, t) = \int_V \alpha \frac{\partial^2 p_p(\mathbf{r}, t)^2}{\partial t^2} g(\mathbf{R}, \mathbf{r}) d\mathbf{r}$$

## Channel Modelling

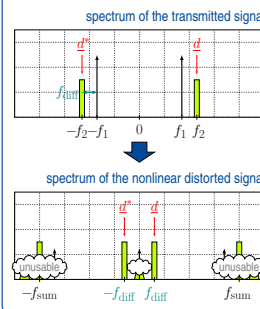
- the above discussed solution can be represented in a block-oriented channel model
- the consideration of only one virtual point source gives the channel model [2]:



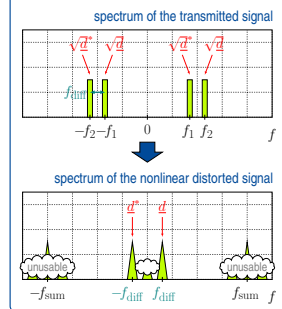
- **derived channel model:** → special case of the Hammerstein model
- can be used in order to investigate modulation techniques

## Modulation Techniques

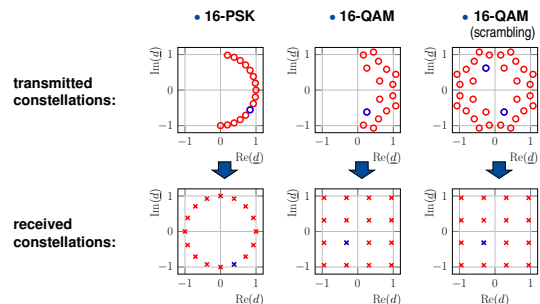
- **conventional approach**



- **modulation by predistortion**



## Constellations



## Conclusion

- the modulation techniques utilise the channel nonlinearity in order to generate conventional signal forms
- the modulation by predistortion outperforms the conventional approach for  $M$ -QAM schemes [3]
- both modulation techniques achieve the same performance for  $M$ -PSK schemes

[1] P. J. Westervelt: Parametric Acoustic Array. Journal of the Acoustical Society of America, vol. 35, no. 4, pp. 535-537, 1963.  
 [2] K. Wiedmann, T. Weber: A Grey-Box Modelling Approach for the Nonlinear Parametric Channel. IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP'14), pp. 4327-4331, Florence, Italy, 2014.  
 [3] K. Wiedmann, T. Weber: Comparison of Modulation Techniques for Parametric Underwater Communications. International Conference and Exhibition on Underwater Acoustics (UA2014), pp. 1443-1448, Rhodes, Greece, 2014.